

Ballooning Modes in Thin Accretion Disks*

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Abstract

In astrophysical accretion disks, the observed rate of angular momentum transport is often explained by appealing to turbulence excited by plasma collective modes such as the Magneto-Rotational Instability,^{1,2} originally derived as “long-cylinder” modes in a differentially rotating MHD fluid. When confined to a geometrically thin disk, however, these axisymmetric modes instead become of the ballooning type³ and take on a much more limited character with a discrete spectrum and reduced growth rates, as shown by Coppi & Coppi.⁴ Their excitation requires that the magnetic energy be considerably lower than the thermal energy, and while they are well-localized in the vertical direction, they acquire a characteristic oscillatory profile in the radial direction, leaving open the problem of identifying a physical factor which can make them radially localized.

The normal mode equation describing the modes is derived, and its solutions are shown to be of two types: a discrete spectrum of modes which are vertically well-localized compared to the disk height, and a continuous spectrum of quasi-localized modes which decay more slowly at the boundaries of the disk but which may leave open the possibility of constructing wave packets for radial localization. However, the power-law profiles of the quasi-localized modes are too gradual to be physically realistic except possibly in a narrow range of mode wavelengths for cases where the magnetic energy is extremely small.

We are currently verifying these results through numerical simulations of thin Keplerian MHD disks, a case that has not often been treated in other simulations in the field, which typically use vertically periodic or “fat torus” geometries.

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¹ Velikhov, E.P. 1959, *Soviet Phys, JETP*, **36**, 995

² Balbus, S.A., and Hawley, J.F. 1991, *Ap J*, **376**, 2

³ Coppi, B. 1977, *Phys Rev Let*, **39**, 939

⁴ Coppi, B., and Coppi, P.S. 2001, *Phys Rev Let*, **87**, 5, 051101-1