

# Dynamic Electrical Conductivity In A Bumpy Cylinder Magnetic Field\*

A. L. García-Perciante, J. D. Callen, K. C. Shaing and C. C. Hegna

University of Wisconsin-Madison, Madison WI 53706-1609

In the banana collisionality regime, the parallel electrical conductivity in a toroidal plasma is affected by interactions between trapped and passing particles. In a fluid moment approach this effect is introduced through the parallel viscous force  $B \cdot \nabla \cdot \Pi$ . What we seek here, is a functional form for this term for a dynamically varying case. The equilibrium and time dependent cases have been dealt with by various authors [1]-[5] with different approaches and results. We present a discussion of these procedures as well as advances in a new model based on a Chapman-Enskog-like approach [4, 5].

In the spirit of developing an appropriate expression for this parallel viscous force, we consider the simple case of a cylindrical magnetic field with periodic bumps. The viscous force in equilibrium ( $\frac{\partial}{\partial t} \rightarrow 0$ ) has already been solved and recovers the known result. For the dynamic problem, an eigenmode expansion procedure already developed [6] has been used. We present a deductive approach within this context based on a large aspect ratio expansion that simplifies the response. High and low frequency limits relative to the collision frequency are being investigated.

The calculation seeks a real space, time-dependent analytical solution, convenient for facilitating use in future numerical computations in codes like NIMROD. A transformation to frequency space makes it possible to compare the results for relaxation rates with those in the literature mentioned above.

\*Research supported by DoE grant DE-FG02-86ER53218.

## References

- [1] F. L. Hinton and R. D. Hazeltine, *Rev. Mod. Phys.* **48**, 239 (1976).
- [2] S. P. Hirshman and D. J. Sigmar, *Nucl. Fusion* **21**, 1079 (1981).
- [3] F. L. Hinton and C. Oberman, *Nucl. Fusion* **9**, 319 (1969).
- [4] J.P. Wang and J.D. Callen, *Phys. Fluids B* **4**, 1139(1992).
- [5] J.P. Wang and J.D. Callen, *Phys. Fluids B* **5**, 3207 (1993).
- [6] C.T. Hsu, K.C. Shaing and R. Gormley, *Phys. Plasmas* **1**, 132 (1994).