

## Impact of field line label and ballooning parameter on infinite- $n$ ballooning stability in compact stellarators\*

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The infinite- $n$  ideal ballooning mode stability of a non-axisymmetric equilibrium is a function of the ballooning parameter,  $\theta_k = k_r/k_\alpha$  and the field line label,  $\alpha = \theta - \iota\xi$ . Here,  $k_r$  and  $k_\alpha$  are the components of the wavenumber perpendicular to the magnetic field and  $\iota$  is the rotational transform. In this work, the impact of field line label and ballooning parameter on the infinite- $n$  ballooning stability of compact, quasi-poloidal symmetric stellarators is investigated. Previously, the ballooning stability of quasi-poloidal stellarators has been examined for fixed-boundary, very-high  $\beta$  ( $\beta > 10\%$ ), tokamak-stellarator hybrid configurations [1] and free-boundary, moderate  $\beta$  ( $\beta > 4\%$ ) plasmas in the Quasi-Poloidal Stellarator (QPS) [2]. These previous calculations were performed with  $\theta_k$ ,  $\alpha = 0$ . Here, these results are extended to include other possible values of  $\theta_k$  and  $\alpha$ . The first ballooning instability  $\beta$ -limits for these devices are well described by the  $\theta_k$ ,  $\alpha = 0$  results. Changing either  $\theta_k$  or  $\alpha$  increases the  $\beta$  required for first instability. The  $\beta$  values required to enter second ballooning stability are higher when  $\theta_k$ ,  $\alpha \neq 0$ . The plasma is still first-unstable to modes with  $\theta_k$ ,  $\alpha \neq 0$  even after modes with  $\theta_k$ ,  $\alpha = 0$  (and regions nearby in parameter space) become second stable. These results are compared with calculations of the stability of finite- $n$  ballooning modes in both the hybrid configuration and the QPS configuration.

\*This work is supported by the U.S. DOE under grant No. DE-FG02-03ER54699 at the University of Montana.

[1] A. S. Ware, S. P. Hirshman, D. A. Spong, et al., Phys. Rev. Lett. **89**, 125003 (2002).

[2] A. S. Ware, D. Westerly, E. Barcikowski, et al., "Second ballooning stability in high- $\beta$ , compact stellarators", to appear in Phys. Plasmas (2004).